

An Introduction to Global Atmospheric Modelling

Lecture 2: Introduction Physical Climate Models & Fundamentals Atmospheric Radiation Budget

Content:

- PART 1: Introduction Physical Climate Models
- PART 2: Basics of Atmospheric Radiation
- PART 3: Numerical formulation in Global Models
- PART 4: Daisy World



Institut für
Physik der Atmosphäre

Veronika Eyring
DLR - Institut für Physik der Atmosphäre
Oberpfaffenhofen

Outline

Radiative Processes, page 2

- Lecture 1 (27 April): Introduction to Global Atmospheric Modelling
- Lecture 2 (04 May): Physical Climate Models & Fundamentals Atmospheric Radiation

Preliminary schedule:

- Lecture 3 (11 May): Fundamentals: Chemistry (Aerosols and Gas-phase Chemistry)
- Lecture 4 (18 May): Fundamentals: Dynamics of the Atmosphere
- Lecture 5 (25 May): Introduction into NCAR Command Language (NCL)
- Lecture 6 (1 June): NCL practice (Dr. Mattia Righi) **Doppelstunde**
- Lecture 7 (8 June): moved to 1 June
- Lecture 8 (15 June): Steps in Model Formulation: Example EMAC
- Lecture 9 (22 June): Model Evaluation and Uncertainties in Climate Projections
- Lecture 10 (29 June): International Climate Modelling Activities: Part 1
- Lecture 11 (6 July): EXAM
- Lecture 12 (13 July): International Climate Modelling Activities: Part 2
- Lecture 13 (20 July): Summary

Final Exam: 6 July 2012, 8:00-10:00

Climate Models

Radiative Processes, page 3

Simulate behavior of climate system, ultimate objective

- Understand key physical, chemical and biological processes that govern climate
- Obtain a clearer picture of past climates by comparison with empirical observation
- Project future climate change

Models simulate climate on a variety of spatial and temporal scales

- Regional climates
- Global-scale climate models - simulate the climate of the entire planet

Processes that must be considered when constructing a climate model

1. **Radiative** - the transfer of radiation through the climate system (e.g. absorption, reflection);
2. **Dynamics** - the horizontal and vertical transfer of energy (e.g. advection, convection, diffusion);
3. **Surface process** - inclusion of processes involving land/ocean/ice, and the effects of albedo, emissivity and surface-atmosphere energy exchanges
4. **Chemical** - for a chemistry-climate model (CCM) or ESM with chemistry
5. **Carbon** - for an ESM (defined as AOGCM + carbon cycle + other components)

Three-Dimensional Models - AOGCM

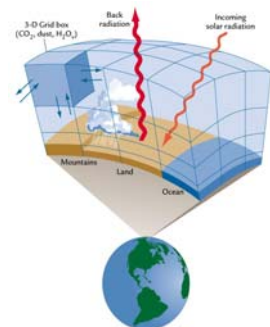
Radiative Processes, page 4

3-D representation of Earth's surface and atmosphere

Most sophisticated attempt to simulate the climate system (except ESM)

3-D model based on fundamental laws of physics:

- Conservation of energy
- Conservation of momentum
- Conservation of mass
- Ideal Gas Law



Constructing Climate Models

Radiative Processes, page 5

Basic laws and relationships necessary to model the climate system are expressed as a series of equations which may be

- Empirical derivations based on relationships observed in the real world
- Primitive equations that represent theoretical relationships between variables
- Combination of the two

Equations solved by finite difference methods

- Must consider the model resolution in time and space *i.e.* the time step of the model and the horizontal/vertical scales

All models must simplify complex climate system

- Limited understanding of the climate system
- Computational restraints

Simplification may be achieved by limiting

- Space and time resolution
- Parameterization of the processes that are simulated

Parameterization

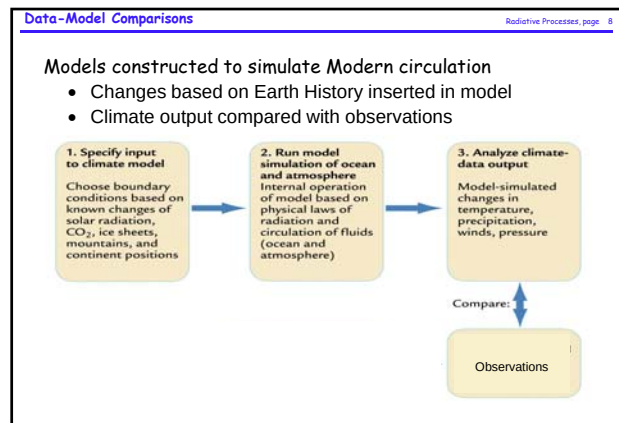
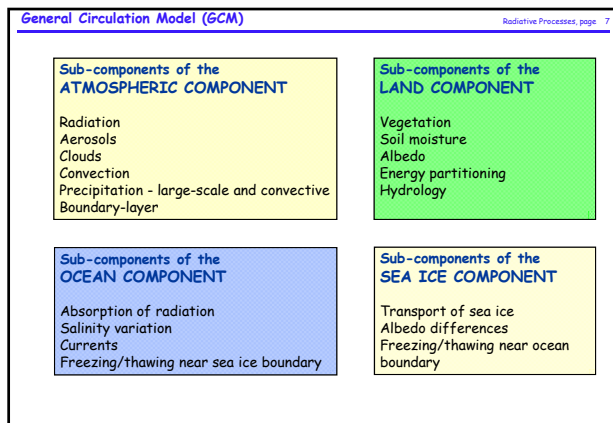
Radiative Processes, page 6

Involves inclusion of a process as a simplified function rather than an explicit calculation from first principles

- Sub-grid scale phenomena, like thunderstorms, must be parameterized
 - Not possible to deal with these explicitly
- Other processes are parameterized to reduce computation required

Certain processes omitted from model if their contribution negligible on time scale of interest

- Role of deep ocean circulation while modeling changes over time scales of years to decades
- Models may handle radiative transfers in detail but neglect or parameterize horizontal energy transport
- Models may provide 3-D representation but contain much less detailed radiative transfer information

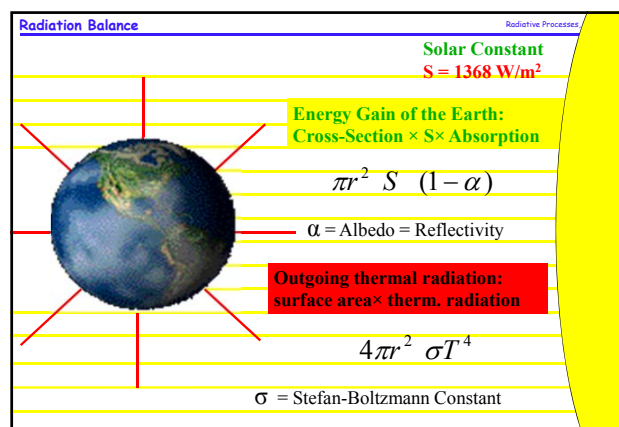


Climate Physics: Lecture on Radiation Processes

PART 2
Basics of Atmospheric Radiation

Overview

- Radiation Laws (Emission)
 - Planck's Law
 - Wien's Displacement Law
 - Stefan Boltzmann Law
- Absorption, Scattering, Reflection
- Radiative Transfer Equation



Natural Greenhouse effect Radiative Processes, page 11

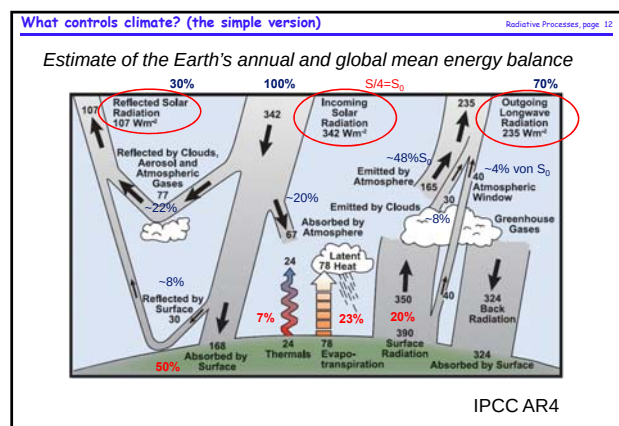
$$\pi r^2 (1 - \alpha) S = 4\pi r^2 \sigma T^4$$

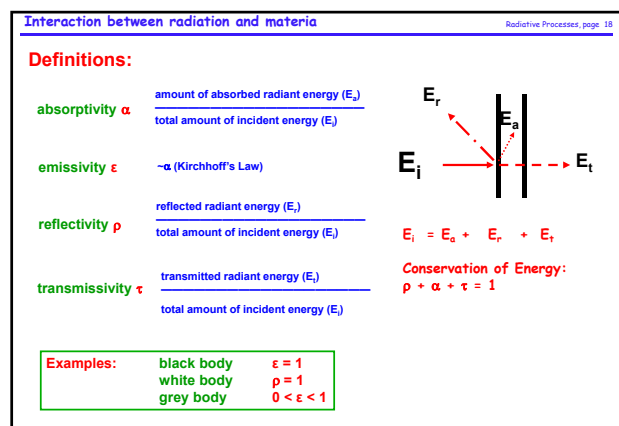
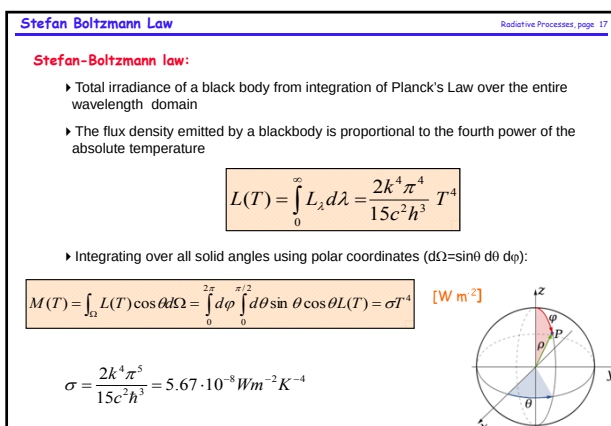
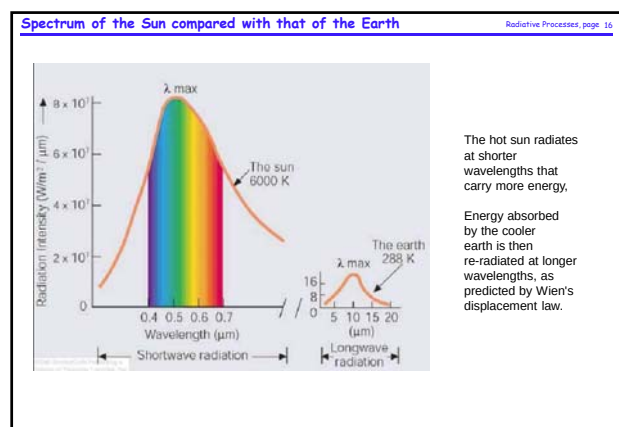
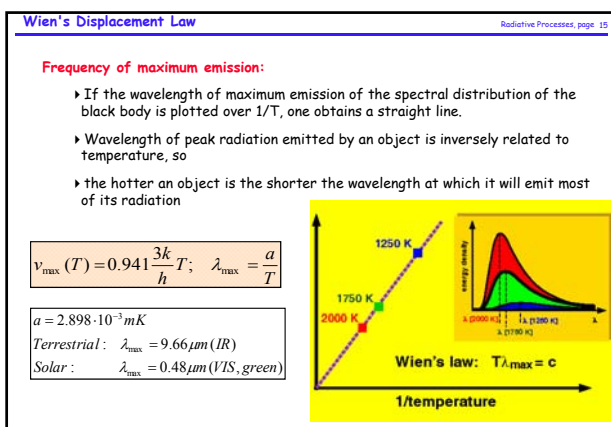
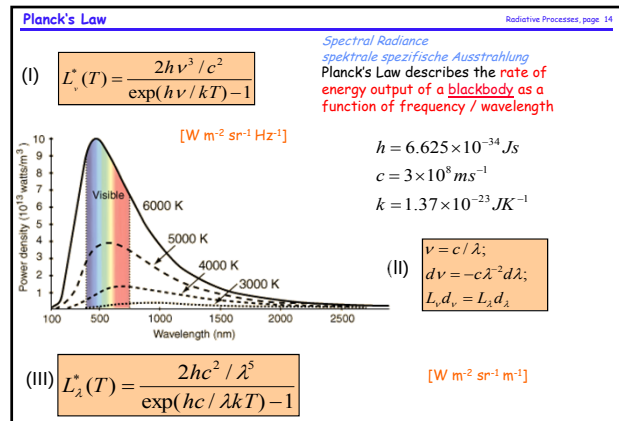
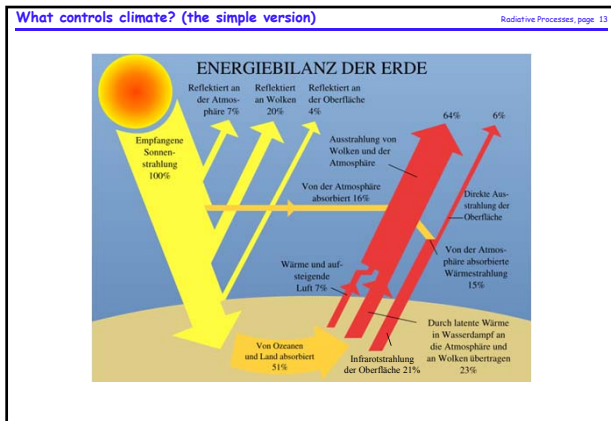
Radiation Temperature:

$$T = \sqrt[4]{S(1 - \alpha) / (4\sigma)}$$

Earth:
 $S = 1368 \text{ Wm}^{-2}$
 $\alpha_e = 0.3$
 Therefore:
 $T_e = 255\text{K} = -18^\circ\text{C}$

The natural greenhouse effect causes the mean temperature of the Earth's surface to be about 33°C warmer than it would be if natural greenhouse gases were not present.





Absorption of Radiation by Molecules

Radiative Processes, page 19

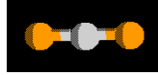
Rotational modes:

- atoms of a molecule rotate around axis
- important for absorption of longwave radiation
- usually requires low energies



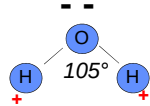
Vibrational modes:

- atoms of a molecule "wobble"
- important for absorption of longwave radiation
- occurs at higher energies than rotational bands



Rotational and vibrational modes

- require a permanent dipole moment (uneven distribution of electrons) to produce oscillating electric dipole moment and therefore affection transmission of electromagnetic radiation
- mainly found in molecules with three atoms, e.g. H_2O , CO_2

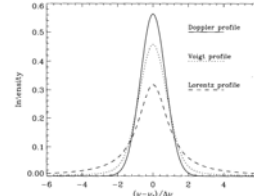


Line Broadening

Radiative Processes, page 20

Instead of discrete lines, transitions are observed in a whole wavelength region:

- **Natural broadening:** due to **Heisenberg's uncertainty principle**, limited importance
- **Pressure broadening (Lorentz):** due to collision of molecules or atoms, most important
- **Doppler broadening:** due to Doppler effect (**thermal motion**), important at lower pressure



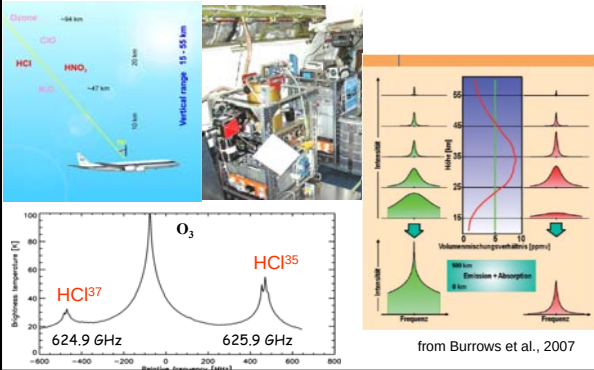
Width of discrete spectral lines in the atmosphere (rotational modes)

Doppler:	$\gamma \approx 1 \text{ MHz}$	Lorentz:	1000 hPa	$\approx 2000 \text{ MHz}$
			100 hPa	$\approx 200 \text{ MHz}$
			10 hPa	$\approx 20 \text{ MHz}$
			1 hPa	$\approx 2 \text{ MHz}$

Measurement of Vertical Profiles

Radiative Processes, page 21

Airborne Submillimeter Radiometer (ASUR), measures between 600 - 700 GHz

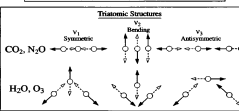


from Burrows et al., 2007

Molecular Absorbers/Emitters in the IR

Radiative Processes, page 22

Molecule	Arrangement	Permanent Dipole Moment
N_2	$\text{N} \equiv \text{N}$	No
O_2	$\text{O} = \text{O}$	No
CO	$\text{C} \equiv \text{O}$	Yes
CO_2	$\text{O} = \text{C} = \text{O}$	No
N_2O	$\text{N} \equiv \text{N} - \text{O}$	Yes
H_2O	$\text{H} - \text{O} - \text{H}$	Yes
O_3	$\text{O} = \text{O} - \text{O}$	Yes
CH_4	$\text{C} - \text{H}_4$	No



- Molecules of gas in the atmosphere interact with photons of electromagnetic radiation
- Different kinds of molecular transitions can absorb/emit very different wavelengths of radiation
- Some molecules are able to interact much more with photons than others

CO_2 :

- NIR + vib-rot absorption band near $15 \mu\text{m}$ (very important for climate as it occurs near the peak of the terrestrial spectrum)

HO_2 :

- NIR (between 1 and $4 \mu\text{m}$)
- vib-rot band near $6.3 \mu\text{m}$
- densely spaced band of pure rotational lines which strongly absorb terrestrial emission at wavelength in excess of $12 \mu\text{m}$

O_3 :

- in the middle of the water vapor window at $9.6 \mu\text{m}$

Atmospheric Absorption

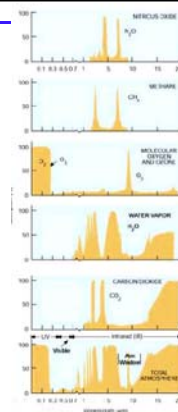
Radiative Processes, page 23

Solar radiation passes rather freely through Earth's atmosphere

Earth's re-emitted longwave energy either fits through a narrow "window" or is absorbed by greenhouse gases and re-radiated toward earth

Major LW absorbers:

Water vapor
 CO_2
 O_3
Clouds

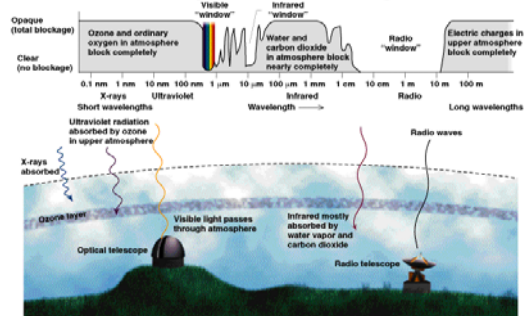


Atmospheric Absorption

Radiative Processes, page 24

Electromagnetic Spectrum

Atmospheric Absorption



What is scattering ? Radiative Processes, page 25

Rayleigh scattering:
The scattering particles are much smaller than the radiation wavelength. Shorter waves are scattered more severely (selective scattering). The power of the scattered wave is $\sim \lambda^{-4}$.

Mie scattering:
The size of the scattering particles (d) is comparable to the radiation wavelength (λ). The power of the scattered wave is very sensitive to the ratio d/λ .

The energy is dispersed in all directions as if the scattering particles act as a new source of radiation.

Scattering Coefficient and Phase Function Radiative Processes, page 26

$$\frac{dL_s}{ds} = -\alpha_s L$$

α_s : scattering coefficient

α_s Scattering coefficient

$P(\gamma)$ Phase function

- > probability of light getting scattered in a single direction
- > Phase function integrates to 1

$\frac{\sigma_s}{4\pi} P(\gamma)$ Light Scattered in any direction (σ_s : scattering cross section units m^2)

σ_s The scattering cross section represents the amount of incident energy which is removed from the original direction due to a single scattering event.

Mie parameter Radiative Processes, page 27

Depending on the ratio of the size of the scattering particle (r) to the wavelength (λ) of the light:

Mie parameter $\alpha = 2\pi r / \lambda$,

Different regimes of atmospheric scattering can be distinguished:

Radiative Transfer Equation (1) Radiative Processes, page 28

Fundamental equation describing the propagation of electromagnetic radiation in a scattering and absorbing medium

$L_\lambda = dL/d\lambda = \text{spectral radiance}$ [Wsr⁻¹m⁻³]

forward

Radiative Transfer Equation Radiative Processes, page 29

Components of Radiative Transfer Equations

Wave attenuation due to absorption

(1) $\frac{dL_A}{ds} = -\alpha_a L$

Loss of energy in the observer's direction due to scattering

(2) $\frac{dL_{S1}}{ds} = -\alpha_s L$

Energy is added in the observer's direction as a result of scattering of waves incident from other directions

(3) $\frac{dL_{S2}}{ds} = -\alpha_s \tilde{J}(\theta, \phi)$

Energy is added due to thermal emission

(4) $\frac{dL_\epsilon}{ds} = -\alpha_a B(T)$

Figure 8-11. The different elements that contribute to the radiation transfer equation.

Radiative Transfer Equation: Loss Terms Radiative Processes, page 30

Radiative Transfer Equation – Loss Terms

$[-\alpha_a(\lambda) - \alpha_s(\lambda)] L(\lambda, \theta, \phi, s)$

- sum of the absorption coefficients of all the gases and particles in the medium [m⁻¹]
- Scattering coefficient [m⁻¹]

extinction coefficient: $\epsilon^*(\lambda) = \alpha_a(\lambda) + \alpha_s(\lambda)$

$\epsilon^* = \epsilon \rho = \rho (\kappa + \sigma)$ [m⁻¹]

ρ density of the medium [kg m⁻³]

ϵ mass extinction coefficient [m²kg⁻¹]

κ mass absorption coefficient [m²]

σ mass scattering coefficient [m²]

If mixture of gases:

$$\kappa_\lambda = \sum_i \kappa_\lambda^{(i)} \frac{\rho^{(i)}}{\rho}$$

$$\sigma_\lambda = \sum_i \sigma_\lambda^{(i)} \frac{\rho^{(i)}}{\rho}$$

Radiative Transfer Equation: Source Terms Radiative Processes, page 31

Radiative Transfer Equation – Source Terms

$\alpha_s(\lambda) \tilde{J}(\lambda, \theta, \phi) + \alpha_a(\lambda) B(\lambda, T)$
 1 (Scattering) 2 (Emission)

1 Scattering $\tilde{J}(\theta, \phi) = \frac{1}{4\pi} \int_0^{4\pi} L(\theta', \phi') P(\theta', \phi', \theta, \phi) d\Omega'$
scattering phase function

The scattering phase function describes the angular distribution of scattered field
 $(\theta, \phi) \Rightarrow$ incident radiation
 $(\theta', \phi') \Rightarrow$ scattered radiation

2 Emission: Planck's Law

Radiative Transfer Equation Radiative Processes, page 32

$\frac{dL_\lambda}{ds} = [-\alpha_{a,\lambda} - \alpha_{s,\lambda}]L_\lambda + [\alpha_{s,\lambda}\tilde{J}_\lambda + \alpha_{a,\lambda}B_\lambda]$

Losses
Sources

The solution at every point in the medium depends on the interactions between the radiation and the medium at every other point.

$\frac{dL_\lambda}{ds} = -\tilde{\epsilon}_\lambda L_\lambda + J_\lambda(z, \theta, \varphi)$

where J is the sum of both source terms.

The solution of the radiative transfer equation is generally rather complex and can usually only solved numerically. Simplifications exist only for very specific applications and spectral regimes.

Absorption Coefficient Radiative Processes, page 33

$\alpha_{\nu_{ij}} = N \sigma(\nu_{ij}, T) S(\nu_{ij}, P, T)$

N: Number Density [Particles cm⁻³]
 $N = \frac{n}{V} = \frac{p_{partial}}{kT} = \frac{VMR \cdot p_{partial}}{kT}$

σ : Absorption Cross Section [cm² Particles⁻¹]
 JPL Catalogue $\sigma(\nu_{ij}, T)$

S: Line Broadening

- Natural Broadening** $\Delta E \Delta t \approx \frac{h}{2\pi}$ $\Delta t \approx \frac{h}{2\pi \hbar \Delta \nu}$ $\approx \frac{1}{2\pi \Delta \nu}$
- Doppler Broadening** Second major source of line broadening. Molecules are in motion when they absorb. This causes a change in the frequency of the incoming radiation as seen in the molecules frame of reference
- Pressure Broadening** Line width depends on the number of collisions per second, i.e. on the number density of the molecules (Pressure) and the relative speed of the molecules (the square root of the temperature)

Moleküle besitzen für elektromagnetische Wellen einen Absorptionskoeffizient. Der Absorptionskoeffizient ist wellenlängenabhängig. Die absorbierten Lichtwellen erzeugen in den Gasmolekülen: Rotation, Vibration $\Rightarrow$ Wärme angeregte Zustände $\Rightarrow$ Lichtwellen anderer Wellenlänge. Der Absorptionskoeffizient wird in 1/m angegeben, d.h. welcher Anteil der Intensität pro Meter Gas (bei bestimmten Druck) absorbiert wird.

Approximations to solve RTE Radiative Processes, page 34

Plan-parallel (SZA < 75°)

Abbildung 1.4: Darstellung des Strahlungsantriebs in sphärischer Geometrie

Basic Steps in a GCM radiation scheme Radiative Processes, page 35

- Formal Solution of the RTE**
- Vertical integration**
 - i.e. accounting for the variations in **temperature, pressure** and density of radiatively **active absorbers and scatterers**
 - gives a directional quantity called **monochromatic radiance**
- Integration over solar zenith angle**
 - gives a **monochromatic irradiance**
- Spectral Integration**
 - i.e. an integration over the relevant part of electromagnetic spectrum (LW, SW)
 - gives a **total flux**
- Differentiation of the Vertical Component**
 - to get the radiative heating/cooling rate

Mote and O'Neill

Parameterisation of atmospheric radiation Radiative Processes, page 36

The object of any parameterisation of atmospheric radiation for use in an atmospheric circulation models is to provide a simple, accurate and fast method

- Calculation must supply:**
 - Total radiative flux at the surface (to calculate the surface energy balance)
 - Vertical and horizontal radiative flux divergence to calculate radiative heating and cooling rates of an atmospheric volume
- Parameterization should include**
 - absorption and scattering by absorbing gases, clouds and haze particles
- Trade off between accuracy and speed**
 - Level of approximation and level of speed determine the interactions between radiation and dynamics
 - Radiation affects dynamics
 - Dynamics respond to the total heating fields (sum of latent and radiative heating and sensible heating components)

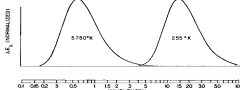
Stephens

Simplifications of radiative computations in global models Radiative Processes, page 37

- E.g., Plane-parallel assumption
- Gas constituents are homogeneously mixed within each cell
- Separation between Shortwave (SW) and Longwave (LW) radiation schemes owing on the obvious difference between a black-body at the Sun's temperature (T~5800K) and that of the atmosphere (T~255K seen at TOA)

SW: most of its energy below 4μ

LW: most of its energy above 4μ


- Computation of radiation less frequently called than dynamics
 - typical radiation time step: 2 hours
 - typical dynamical time step: 30 minutes

ECHAM5

Heating Rates Radiative Processes, page 38

- SW and LW separated on the basis of wavelength
 - computation in LW and SW in spectral bands
 - LW: scattering is neglected
- Computing of radiative heating and cooling rates
 - usually done by calculations of upward and downward fluxes through unit horizontal areas, taking into account the vertical distributions of temperature, water vapour and other radiatively active gases (e.g. CO₂, O₃).
 - Total Flux: $F_{\text{rad}} = F_{\text{LW}} + F_{\text{SW}}$
 - Radiative heating rates Q are calculated from the difference of the total flux F_{rad} at the lower and upper boundary of a cell, the amount of air m and the specific heat c_p of moist air

$$Q_{\text{rad}} = -(F_{\text{rad}}^{\text{lower}} - F_{\text{rad}}^{\text{upper}}) / (m \cdot c_p)$$

$$c_p(t) = (1 - q_v(t)) \cdot c_{p,d} + q_v(t) \cdot c_{p,v}$$

$$m = (p_{\text{lower}} - p_{\text{upper}}) / g$$

ECHAM5 / Washington and Parkinson

Photolysis Rates Radiative Processes, page 39

See also Lecture on Chemistry

First order reaction

$A + h\nu \rightarrow C + D$

Time Dependence for A (J is the photolysis frequency [s⁻¹]):

$$\frac{d[A]}{dt} = -J[A]$$

Example:

$$O_2 + h\nu (\lambda < 242\text{nm}) \rightarrow 2 O$$

Photolysis Reaction Rates Radiative Processes, page 40

Species A undergoes photodissociation.

Reaction i : $A + h\nu \rightarrow \text{products}$

A absorption cross section

Reaction i quantum yield

Wavelength

$$\left. \frac{d[A]}{dt} \right|_{\text{reac } i} = -[A] \cdot \underbrace{\int \sigma_X(\lambda) \phi_i(\lambda, T, \dots) E(\lambda, \dots) d\lambda}_{\text{Action spectrum}} \underbrace{\quad}_{\text{Spectral actinic flux}}$$

Reaction rate coefficient J

$$J = \int \sigma(\lambda) \phi(\lambda) \int_{\omega} I(\lambda, \theta, \phi) d\omega d\lambda$$

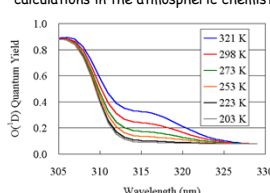
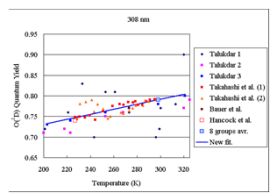
A concentration rate of change due to photolysis reaction i

Quantum Yield Radiative Processes, page 41

Example for Quantum Yield: $\sum \phi_i = 1$, where summation is over all possible pathways
 $\phi_A = \sum \phi_{i,A}$, where summation is over all pathways that yield A

Photolysis of O₃ + hν (λ < 325 nm) → O(¹D) + O₂

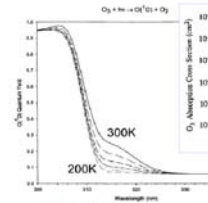
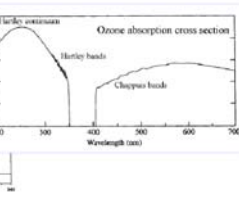
The quantum yield for O(¹D) production in the photolysis of ozone in the ultraviolet region as a function of wavelength and temperature is a key input for modeling calculations in the atmospheric chemistry.

http://www.sparc.sunysb.edu/html/QY_O1D/

Ozone photolysis Radiative Processes, page 42

Ozone photolysis

O₃ + hν → O(¹D) + O₂

O₃ + hν → O(³P) + O₂ λ < 800 nm

O₃ + hν → O(¹D) + O₂ λ < 320 nm

It is important to distinguish the **actinic flux** from the **spectral irradiance**, which refers to energy hitting a flat surface having fixed spatial orientation ($\text{J m}^{-2} \text{nm}^{-1}$)

• The **actinic flux** does **not refer to any specific orientation** because molecules are oriented randomly in the atmosphere.

• This distinction is of practical relevance: the actinic flux (and therefore photolysis) **near a brightly reflecting surface** (e. g. over snow or above a thick cloud) can be a factor of **three higher** than that near a non- reflecting surface.

Radiance I_λ Energy flux per solid angle ($\text{W m}^{-2} \text{sr}^{-1} \mu\text{m}^{-1}$)

Irradiance F_λ : Radiance integrated over all solid angles

($\text{W m}^{-2} \mu\text{m}^{-1}$)

Actinic flux $F(\lambda) \equiv \int_{\omega} I(\lambda, \theta, \phi) d\omega = \int_{\phi} \int_{\theta} I(\lambda, \theta, \phi) \sin \theta d\theta d\phi.$

($\text{W cm}^{-2} \text{nm}^{-1}$ or

Photons $\text{s}^{-1} \text{cm}^{-2} \text{nm}^{-1}$)

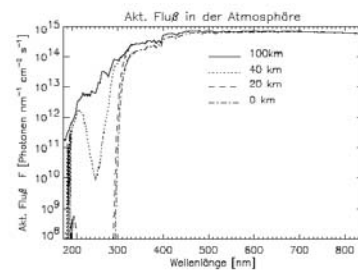


Abbildung 3.2: Aktinischer Fluß innerhalb der Atmosphäre bei 60° Sonnenzenitwinkel, Albedo = 0.3, US-Standard Atmosphäre [Anderson et al. (1986)], Sonnenspektrum nach WMO (1985).

Global Modelling: Lecture on Daisyworld



PD Dr. habil. Veronika Eyring
DLR - Institut für Physik der
Atmosphäre, Oberpfaffenhofen

Overview

- 1 Introduction
- 2 Daisyworld Description
- 3 Modelling Daisy World
 - Population Dynamics
 - Energy Balance
 - Numerical Solution
- 4 Example

Introduction

A new theory of how the world works...

- In 1965, James Lovelock, a atmospheric chemist, was thinking about why life evolved on earth and not on Mars or Venus
- Why has temperature of earth's surface remained in narrow range for last 3.6 billion years when heat of sun has increased by 25%?

Answers:

- Difficult to understand without considering role of life
- We understand that abiotic (non-living) factors (physical, geological and chemical) determine biological outcomes
- New idea is that Biotic (living) factors feedback to control abiotic factors.
- Example of a negative feedback:



Gaia Theory and Daisyworld

Gaia Theory: Maintenance of Surface Temperatures

- **Gaia: Greek for 'Mother Earth'**: complex entity involving the Earth's biosphere, atmosphere, oceans, and soil.
- **According to Lovelock**, "Gaia theory predicts that the climate and chemical composition of the Earth are kept in homeostasis for long periods until some internal contradiction or external force causes a jump to a new stable state."
- According to Gaia, life regulates surface temperature because it has remained within 10-20°C for over 3 billion years.
- This is remarkable because the sun's output has increased by 30% or 40%.

Daisyworld: A simple heuristic mathematical model [Watson and Lovelock (1983)]

To demonstrate the principle of biological homeostasis

- Automatic stabilization a planet's temperature in the face of increased solar luminosity through biological feedbacks
- Biological feedbacks arising out of natural selection alone.



Daisyworld Description

A long time ago, in a galaxy far, far away...

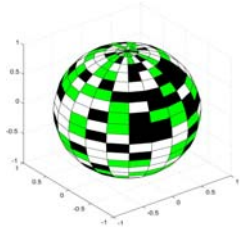
Daisyworld is an imaginary planet

- of same size, rotation, distance from the Sun as Earth
- Sun of the same mass and luminosity as our sun,
- **Cloudless, no greenhouse gases, more land than ocean area.**
- Fertile, well watered soil, plants will grow anywhere if the temperature is right
- **The planet is flat**, resulting in similar changes in temperature with changing solar luminosity (energy from the sun) and albedo being experienced simultaneously over its surface, and does not experience any seasonality in climate.
- The composition of the planet's biota is similarly lacking in complexity
 - * 2 daisy species (light and dark colored flowers)
 - * All daisies are capable of reproducing.
 - * **Assumed Growth Rate:**
 - Below 5°C, no daisies grow,
 - Over 40°C, all daisies die,
 - 22.5°C is optimal for growth of all daisies.

Assumptions Daisy World, page 49

- The **rate of population change** for both species of daisy depends on the **death rate** and the **potential birth rate** for that species, and the amount of fertile land available for growth.
- The **birth rate** for both species of daisy depends on the **local temperature** near each daisy type.
- The **local temperature** depends on the **difference between the global and local albedo**, and on the **global temperature**. If the local albedo is large then the local temperature is less than the global temperature.
- The **global temperature** depends on the **luminosity of the Sun and the planetary albedo**.
- The **planetary albedo** is the sum of the **local albedo components** (i.e., the albedo of the black and white daisies and of the bare ground).
- Albedo of White Daisies is 0.75, Black 0.25, and bare ground 0.50.
- By natural selection, the percentage of area covered with black or white daisies varies. This varies total albedo, thus affecting global temperature. Automatic positive and negative feedbacks through natural selection act as a thermostat.

Daisyworld Daisy World, page 50

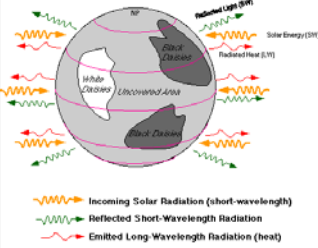


Area	Color	Albedo
F_w	white	$a_w=0.75$
F_b	black	$a_b=0.25$
F_g	green (soil)	$a_g=0.50$

$$F_g + F_w + F_b = 1 \quad \text{total area}$$

$$\alpha_g F_g + \alpha_w F_w + \alpha_b F_b = \alpha \quad \text{global albedo}$$

Schematic Model of Daisyworld Daisy World, page 51



- Black and white daisies
- The temperature is related to how much **solar energy is received** and how much **energy is reflected**
- Amount of energy reflected depends on albedo
- The albedo in turn depends on the coverage by white and black daisies.
- The **heat radiated to space** is a function of how much energy is absorbed.

 Incoming Solar Radiation (short-wavelength)
 Reflected Short-Wavelength Radiation
 Emitted Long Wavelength Radiation (heat)

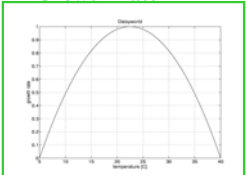
Daisyworld: Population Dynamics Daisy World, page 52

Change of White Area (I) $\frac{dF_w}{dt} = -\gamma F_w + \beta(\theta_w) F_w F_g$

Change of Black Area (II) $\frac{dF_b}{dt} = -\gamma F_b + \beta(\theta_b) F_b F_g$

Ad hoc Death Rate per unit area (constant) γ

Growth Rate $\beta(\theta)$



$$\beta(\theta) = 1 - 0.003265 (22.5 - \theta)^2$$

Daisyworld: Energy Balance Daisy World, page 53

$$\sigma T_e^4 = S(1 - \alpha) \quad S = \text{solar constant} \quad \text{effective temperature of Daisyworld}$$

$$\sigma T_i^4 + N_i = S(1 - \alpha_i) \quad i = w, b, g \quad \text{(III) local balance}$$

Heat transport (from warm to cold, i.e. from black via green to white)

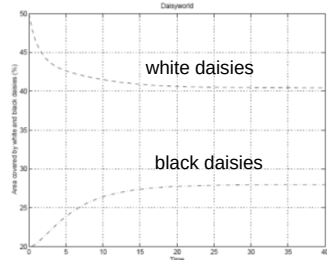
$$N_i = q(\alpha_i - \alpha) \quad -S < q < 0; \quad q = -S: \text{max heat transport} \quad q = 0: \text{zero heat transport}$$

$$\sigma \sum_i F_i T_i^4 = S(1 - \alpha) = \sigma T_e^4 \quad \text{(IV) global balance}$$

$$\alpha_g F_g + \alpha_w F_w + \alpha_b F_b = \alpha \quad \text{global albedo}$$

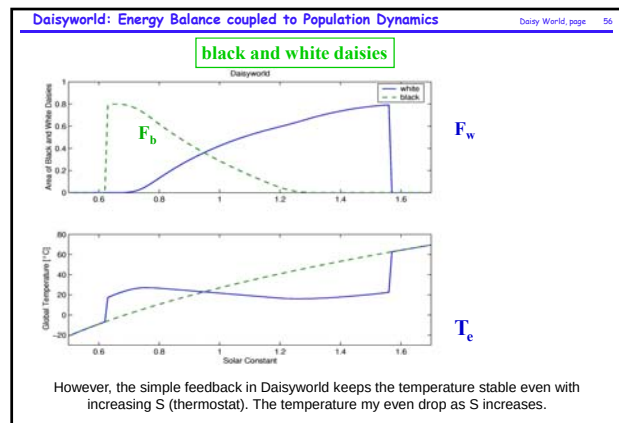
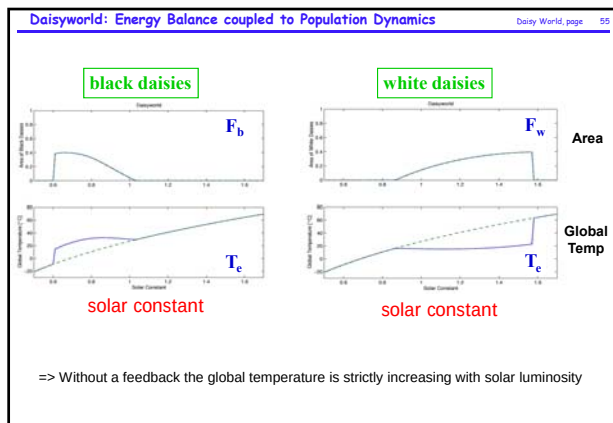
Daisyworld: Numerical Solution Daisy World, page 54

- Now we have all ingredients to solve the system (I), (II), (III) and (IV).
- It is not possible to solve it analytically. Instead, the solution of this rather simple system has to be calculated numerically.
- Solution to the time dependent problem, indicating the evolution towards an equilibrium state



Area in percent

$\gamma = 0.3$
 $S = 917 \text{ Wm}^{-2}$
 $q = -0.9 S$



- Daisyworld: Conclusions Daisy World, page 57
- > The **simple feedback** in Daisyworld keeps the temperature stable even if the solar luminosity varies (thermostat). The temperature may even drop as S increases.
 - > The **black daisies** increase the absorption (and therefore temperature) for a (normalised) solar constant between 0.6 and 1.0 (cold sun), and the **white daisies** reduce very effectively the temperature for values of the (normalised) solar constant between 1.0 and 1.6 (hot sun).
 - > Below values of 0.6 and above values of 1.6 daisies do not grow.
 - > This **thermostat-effect** makes Daisyworld a habitable planet for the two species, for a wide range of flux densities of incoming solar radiation.
 - > In contrast to the positive ice-albedo feedback, the feedback in Daisyworld regulates the temperature. **This negative feedback stabilizes the system.** Positive feedbacks usually have a destabilizing effect.
 - > In some respects this model is typical for the climate and Earth system. Strongly nonlinear components (here the dynamics of the daisy population) are coupled to positive and negative feedbacks which affect the radiation balance of the planet.
 - > Because of the nonlinearity of the system there are multiple solutions (equilibria).

- Erweiterungen des Daisyworldmodells: Thermostat Daisy World, page 58
- Spätere Erweiterungen des Daisyworldmodells schlossen sogenannte Kaninchen, Füchse und andere Arten mit ein, welche Absorptionsraten zwischen denen schwarzen und weißen Daisys haben.
 - Eines der mehr überraschenden Ergebnisse dieser Simulationen war, dass je größer die Anzahl der Arten war, desto größer die selbstregulierenden Kräfte des gesamten Planeten. Dies unterstützte die Ansicht, dass Biodiversität wertvoll ist, und löste die moderne Biodiversitätsdebatte aus.
 - Daisyworld zog auch eine Reihe Kritik auf sich. Es weist kaum Ähnlichkeit mit der Erde auf; das System benötigt eine **Ad-hoc-Todesrate** (γ) um im Gleichgewicht zu bleiben und das Modell verwirft die Unterschiede zwischen Phänomenen auf der Ebene der Arten und jener der Individuen. Jedoch zeigt Daisyworld unbestreitbar, dass biologisch reguliertes Gleichgewicht keine teleologische Erklärung benötigt.
-

Further Reading and Exercise Daisy World, page 59

Animation for Daisyworld:
[_gaia1_Dateien\gaia1.htm](#)

Further Reading:

- > Kirchner, 1989
- > Lovelock, 1989
- > Watson and Lovelock, 1983
- > Dennis Hartmann, Global Physical Climatology, 1994

Further Exercise:

- > <http://cs.clark.edu/~mac/physlets/DaisyWorld/Daisy.htm?l1=0.75&aw=0.2&ab=0.2>
- > <http://www.qingerbooth.com/courseware/daisy.html>

End of Lecture 5 Radiative Processes, page 60

End of Lecture 2